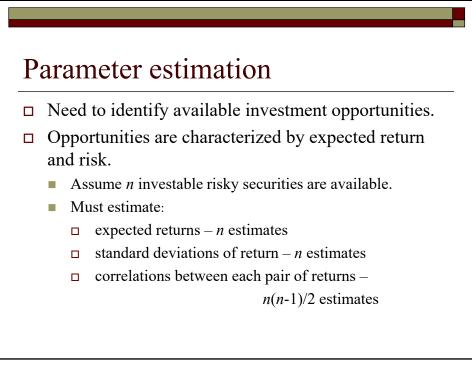
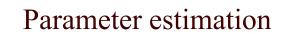


Indifference curves

 Based on properties of indifference curves, riskaverters will maximize expected return for given risk level.

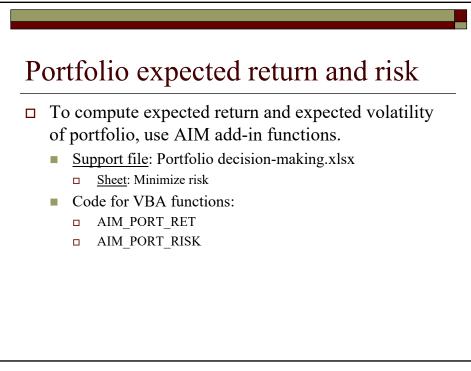
11





□ <u>Notation</u>:

 $E_i \equiv \text{expected return of asset } i$ $\sigma_i^2 \equiv Var(R_i) \equiv Cov(R_i, R_i) \equiv \text{variance of return of asset } i$ $\sigma_i \equiv \sqrt{Var(R_i)} \equiv \text{standard deviation of return of asset } i$ $\sigma_{ij} \equiv Cov(R_i, R_j) \equiv \rho_{ij}\sigma_i\sigma_j \equiv \text{covariance of returns of assets } i \text{ and } j$ $\rho_{ij} \equiv \text{correlation of returns of assets } i \text{ and } j$ $n \equiv \text{number of assets}$ $X_i \equiv \text{proportion of risky asset wealth invested in asset } i$





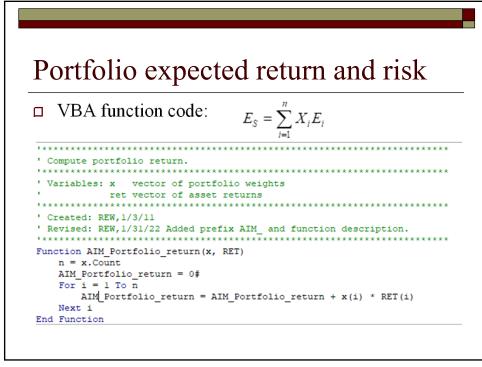


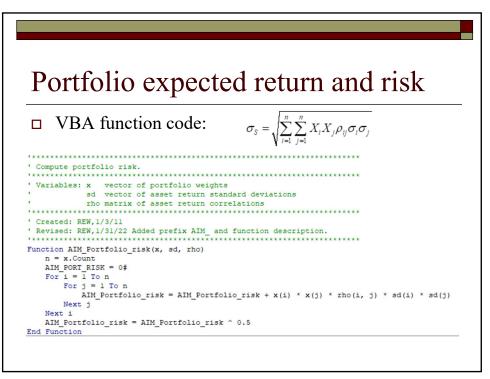
- □ Given estimates of return and risk for individual securities, portfolio (*S*) expected return and risk are defined as:
 - Expected return is

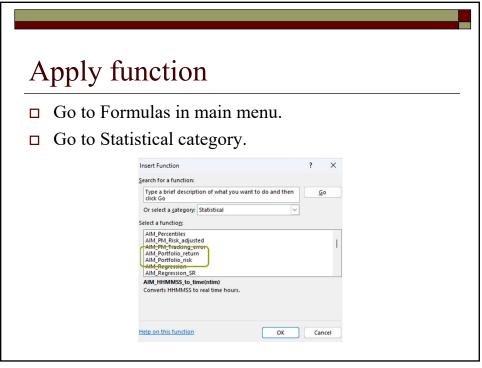
$$E_S = \sum_{i=1}^n X_i E_i$$

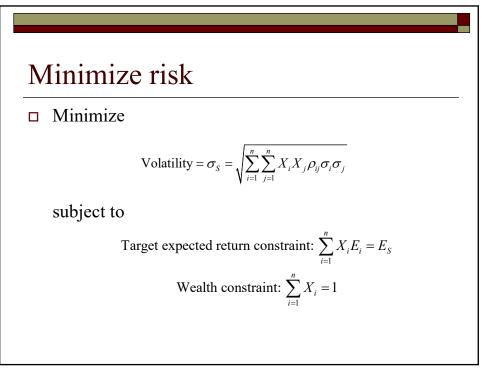
Volatility (or standard deviation) of return is

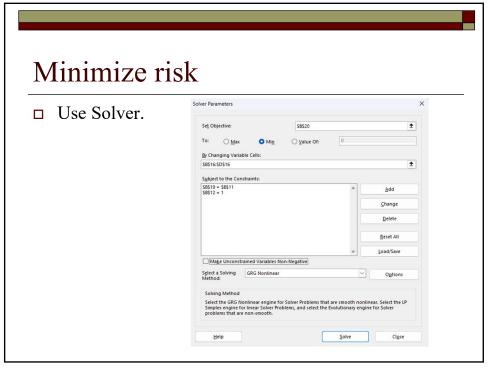
$$\sigma_{S} = \sqrt{\sum_{i=1}^{n} \sum_{j=1}^{n} X_{i} X_{j} \rho_{ij} \sigma_{i} \sigma_{j}}$$



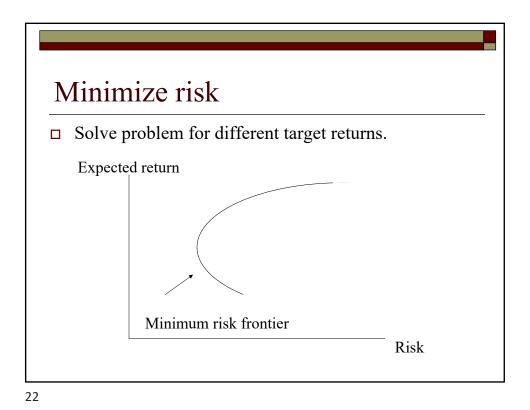


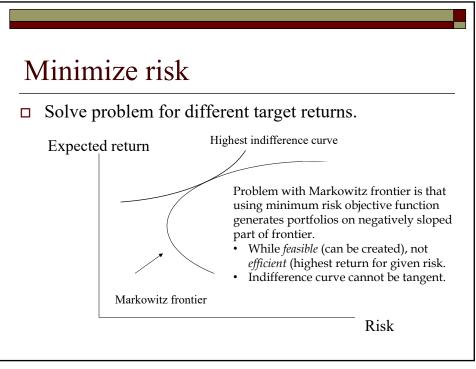


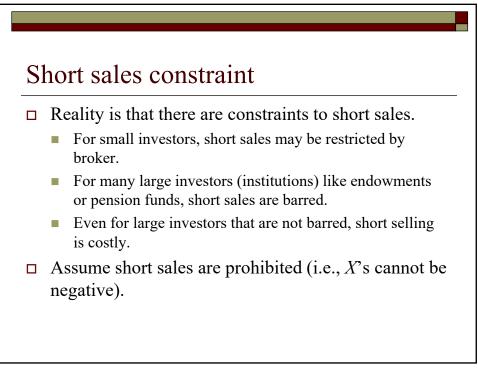


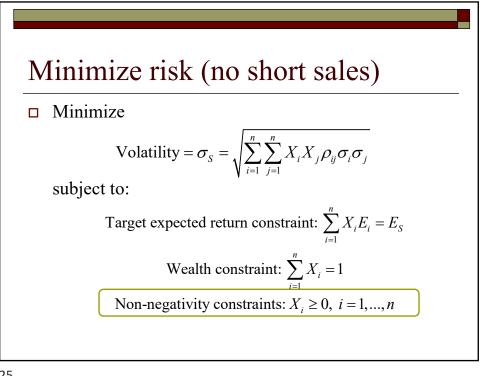


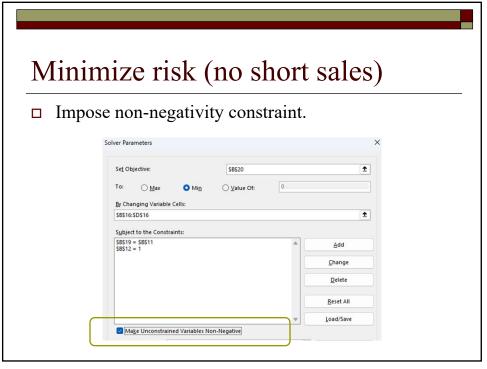
Optin	nal allocations are:
	10 Constraints
	11 Target return 12.00%
	12 Sum of weights 1.000 13 Investment funds 100,000
	14 Final risky asset portfolio (S)
	15 Cash Bonds Stocks
	16 Fractional weights -0.2962 0.9257 0.3705
	17 Dollar investment -29,617 92,568 37,050
	18
	19 Expected return 12.00%
	20 Risk 11.42%

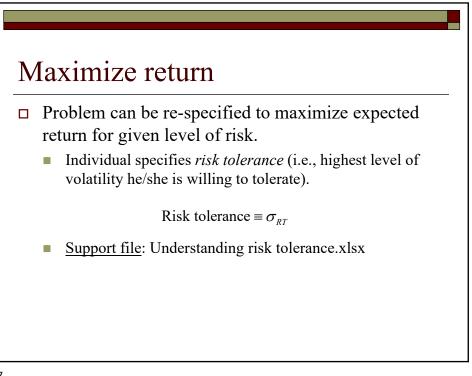


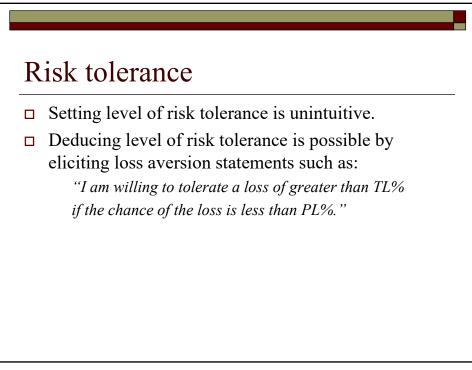




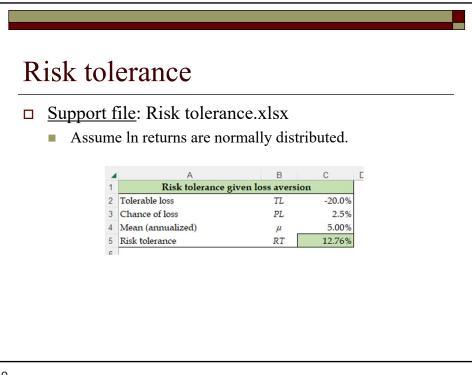


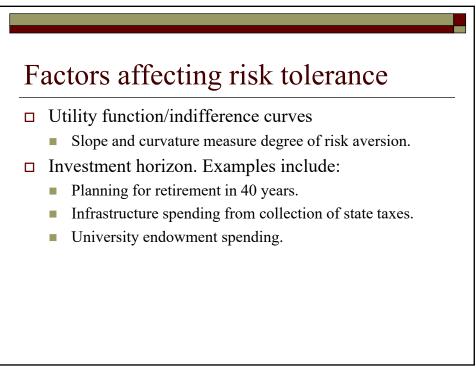




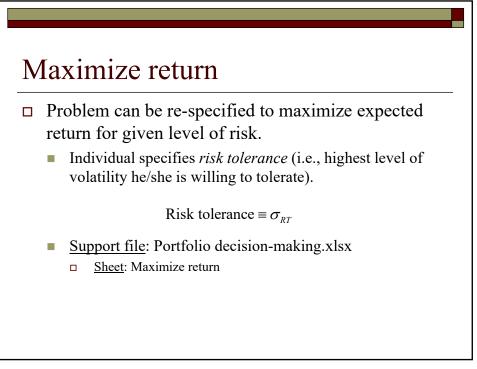


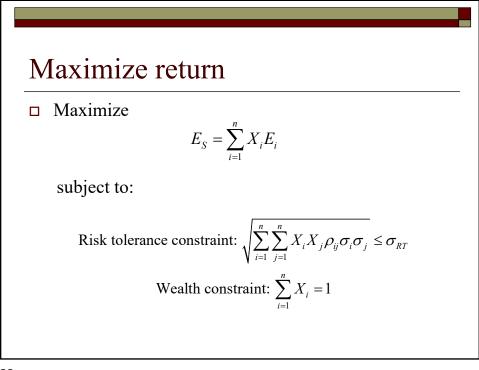


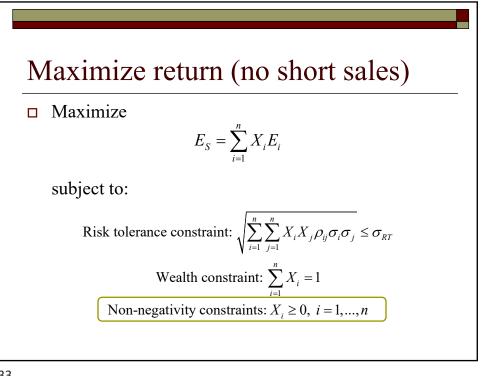


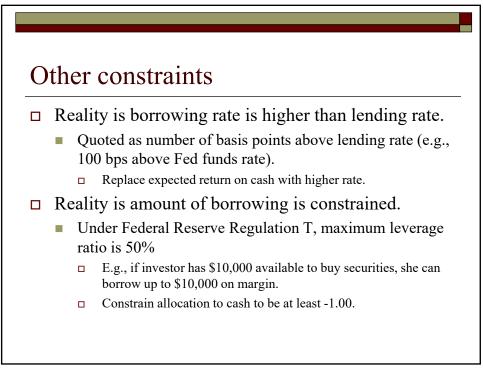










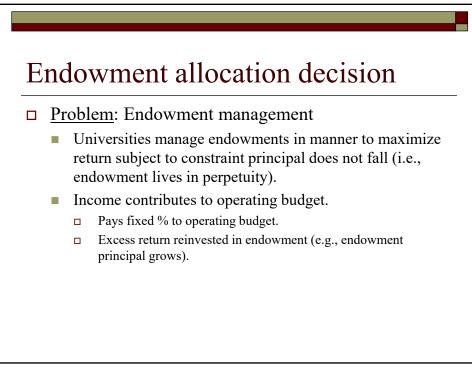


Endowment allocation decision

□ Endowments are:

- Assets (e.g., cash, stocks, bonds) set aside for long-term benefit of organization.
 - Original amount known as "corpus."
- Permanent and will generate income forever.
 - □ Amount of corpus is preserved.





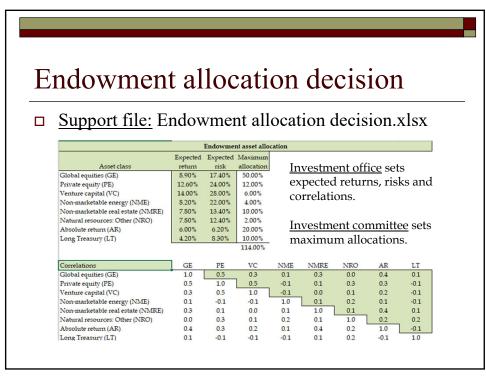


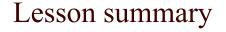


Description: Problem: Endowment management

- Vanderbilt's endowment is about \$6.5 billion.
- In making decision regarding payout, risk tolerance is set to 10.3%.
- About 4.25% of principal is provided to annual operating budgets of schools within university.
- Examine decision made in late 2000s.

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- Portfolio decision-making is based on Markowitz (1952) return-risk mechanics for risky assets.
 - Easily solved using Solver.
- <u>Objective function</u>: Maximize return given risk tolerance.

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